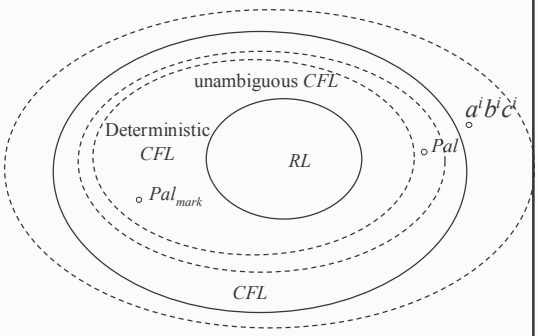
Session 25

Turing Machines
and
Chomsky Hierarchy

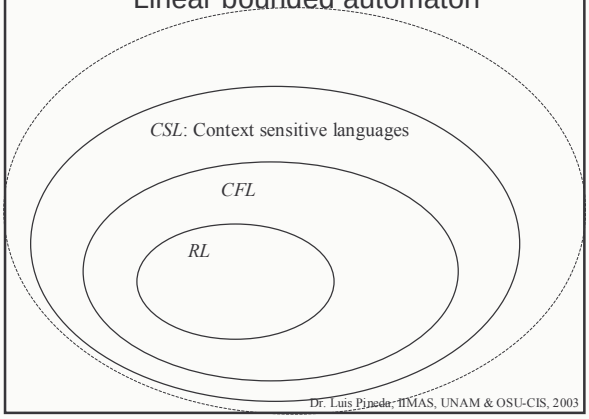
Non-CFL



Two Stacks PDA

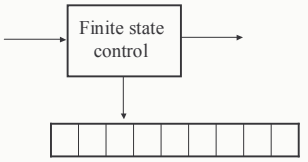
- Processing $a^i b^i c^i$:
  - Push all a's in stack 1
  - For each b pop one a and push a b in stack 2
  - eventually $a^i = b^i$
  - For each c pop one b from stack 2
  - eventually $b^i = c^i$
- But the language is not a CFL
- The 2 stacks PDA is not a PDA

Linear bounded automaton



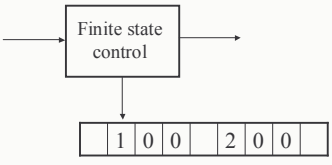
Turing Machine

- Moves: Depending on current state and symbol in the tape:
  - Select next state
  - Write symbol or move left or move right



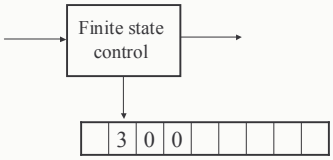
Turing Machine

- Computing a function:
  - Initial state: the arguments



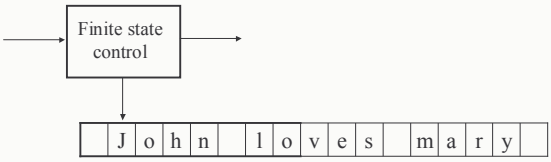
Turing Machine

- Computing a function:
  - Final state: the value



Turing Machine

- Interpreting language is computing a function:



Turing Machine

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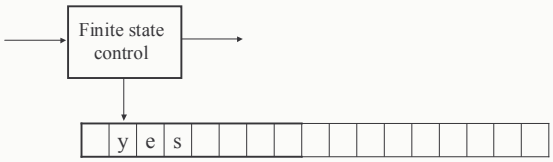

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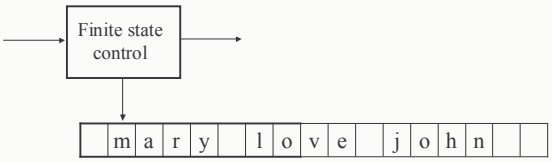

Turing Machine

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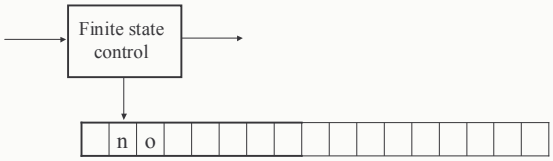

Turing Machine

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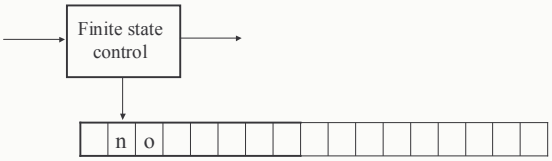
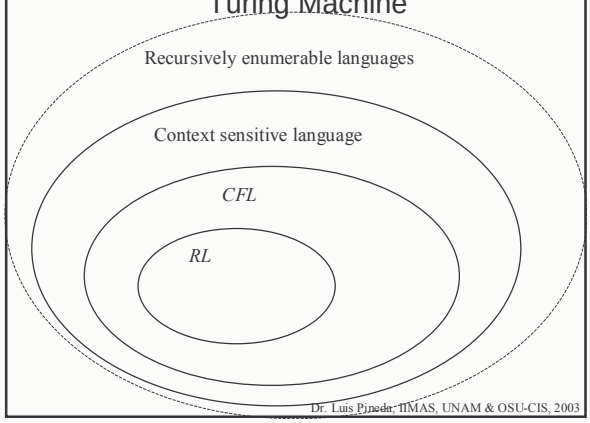
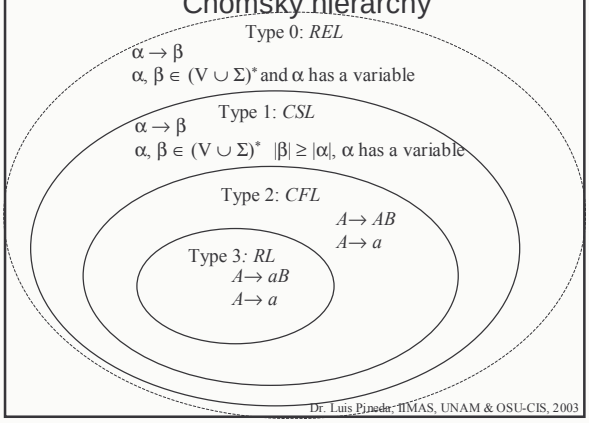


- There is a TM for every function
- Knowing a language is knowing a function!

Turing Machine



Chomsky hierarchy



The halting problem

- If the tape is rewritten we cannot tell whether the computation will ever stop!
- The halting problem cannot be solved by a Turing machine

Church thesis

- The set of function computed by Turing Machines correspond to the set of functions that can be computed intuitively by people
- If a computational device is general enough to compute this set of functions, it is equivalent (can be reduced) to a Turing Machines

Church thesis

- Equivalent formalisms:
  - Turing Machines
  - Theory of Recursive Functions
  - Abacus computation
  - Lambda Calculus